Flexible Multitask Learning with Factorized Diffusion Policy

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Abstract—In recent years, large-scale behavioral cloning has emerged as a promising paradigm for training general-purpose robot policies. However, effectively fitting policies to complex task distributions is often challenging, and existing models often underfit the action distribution. In this paper, we present a novel modular diffusion policy framework that factorizes modeling the complex action distributions as a composition of specialized diffusion models, each capturing a distinct sub-mode of the multimodal behavior space. This factorization enables each composed model to specialize and capture a subset of the task distribution, allowing the overall task distribution to be more effectively represented. In addition, this modular structure enables flexible policy adaptation to new tasks by simply finetuning a subset of components or adding new ones for novel tasks, while inherently mitigating catastrophic forgetting. Empirically, across both simulation and real-world robotic manipulation settings, we illustrate how our method consistently outperforms strong modular and monolithic baselines, achieving a 24% average relative improvement in multitask learning and a 34% improvement in task adaptation across all settings. Website: factorized-diffusion-policy.github.io.

I. INTRODUCTION

The increasing availability of large-scale visuomotor imitation learning datasets has opened new opportunities for training general-purpose robot policies across a wide range of manipulation tasks [1, 2, 3]. However, the inherent diversity and multimodality of these datasets pose major challenges: traditional monolithic policies often struggle to generalize across tasks, represent multiple behavior modes, or adapt efficiently to new skills [2, 4].

To address these limitations, modular policy architectures, most notably Mixture-of-Experts (MoE) models [5, 6], have emerged as a promising direction. By decomposing the policy into specialized components, modular methods improve scalability and reuse across tasks [2, 7, 8, 9, 10]. Yet, existing MoEbased approaches often suffer from training instability [6], lack a principled probabilistic formulation, and produce expert modules with unclear or overlapping roles [8, 11], limiting their interpretability.

We propose *Factorized Diffusion Policy* (FDP), a simple yet effective modular policy architecture. FDP decomposes the policy into multiple diffusion components (Fig. 1a), each capturing a distinct behavioral mode, which are dynamically composed at inference time via an observation-conditioned

router (Fig. 1c). Instead of discrete expert selection as in standard MoE architectures, FDP uses continuous score aggregation, enabling stable training, avoiding routing imbalance, and promoting clearer specialization across components. FDP is grounded in compositional diffusion modeling [11, 12, 13], where aggregating scores corresponds to sampling from the product of distributions, providing a principled probabilistic interpretation and a natural formulation as constraint satisfaction. The modular structure further enables efficient task adaptation: we extend the policy by introducing new diffusion components (Fig. 1b), allowing efficient skill expansion without retraining the entire policy. This factorization improves multitask learning, supports scalable adaptation, and enhances interpretability.

We validate FDP through extensive experiments in simulation benchmarks MetaWorld [14] and RLBench [15], and further demonstrate its practical benefits in real-world robotic manipulation. Our contributions are summarized as follows: (1) We introduce a modular diffusion policy architecture that composes behavior-specialized components via observationconditioned compositional sampling. (2) We demonstrate that our compositional framework improves multitask performance and enables interpretable sub-skill decomposition across diffusion modules. (3) We propose a simple and effective strategy for adapting to new tasks by selectively tuning or augmenting existing components, achieving strong sample efficiency and modular reuse.

II. RELATED WORKS

Diffusion Models for Robotics. Diffusion models have emerged as a powerful tool for modeling complex distributions, achieving strong performance in image [16, 17, 18] and video generation [19, 20]. Their stable training and generative flexibility have led to increasing adoption in robotic domains, including video-conditioned policy learning [21, 22], grasp synthesis [23], trajectory planning [24, 25, 26], and closedloop visuomotor control. Diffusion Policy (DP) [27] demonstrated that diffusion models can be used to learn reactive visuomotor policies from demonstrations, achieving state-ofthe-art performance in single-task imitation learning.

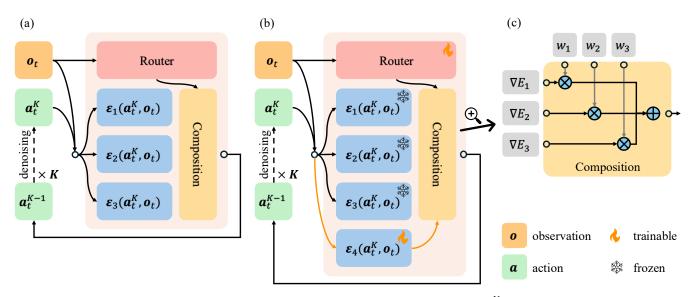


Fig. 1: Overview of FDP. (a) Given an observation o_t , multiple diffusion experts predict score estimates $\varepsilon_i(\mathbf{a}_t^K, \mathbf{o}_t)$ at each denoising step. A lightweight router network computes observation-dependent weights $\{w_i\}$, which are used to compose the final score as a weighted sum (see (c)). The composed score guides the iterative denoising process over K steps to generate an action \mathbf{a}_t . (b) This compositional structure enables FDP to model complex multimodal distributions and supports modular adaptation via selective tuning or addition of diffusion components.

Multitask Imitation Learning and Adaptation. Traditional approaches to multitask imitation learning often rely on monolithic networks [1, 28] or language-conditioned policies [4, 29], which limit scalability, reusability, and interpretability. To address these limitations, Sparse Diffusion Policy (SDP) [8] introduces MoE layers in diffusion models, activating sparse expert sets based on observations. While this modular design enables expert reuse and policy expansion, it suffers from instability and load imbalance [6]. Mixture-of-Denoising-Experts (MoDE) [9] conditions expert routing on noise level, distributing learning across noise levels, making its experts less interpretable or transferable across tasks. In contrast, FDP composes diffusion models through continuous score aggregation, avoiding hard expert selection and ensuring all components are jointly optimized. This promotes stable optimization, clear specialization, and better load balancing. While maintaining modular extensibility like MoE designs, FDP allows efficient adaptation by adding new components without overwriting prior skills.

III. FDP: FACTORIZED DIFFUSION POLICY

We aim to develop a modular policy architecture that scales to diverse manipulation tasks and supports efficient adaptation to new ones. Traditional monolithic policies struggle with the complexity and multimodality of real-world action distributions, while modular alternatives like Mixture-of-Experts (MoE) suffer from training instability and poor expert interpretability. Our proposed FDP, which directly factorizes the policy into a set of composable diffusion models. Each component captures a distinct behavioral mode, and the final action is produced via a weighted aggregation of these modules conditioned on the current observation (Fig. 1).

A. Probabilistic Policy Modeling

We factorize the action distribution as the product of a set of composed distributions

$$p(\mathbf{a}_t|\mathbf{o}_t) \propto \prod_i p_i(\mathbf{a}_{t,i}|\mathbf{o}_t)^{w_{t,i}},$$
 (1)

where $\{w_{t,i}\}\$ are observation-dependent weights associated with each component distribution. Intuitively, $p(\mathbf{a}_t|\mathbf{o}_t)$ represents the intersection (logical AND) of individual distributions, assigning high likelihood to samples commonly favored by all component distributions. Moreover, each diffusion component $p_i(\mathbf{a}_{t,i}|\mathbf{o}_t)$ can be interpreted as imposing a behavioral constraint (e.g., collision avoidance, precise grasping) [30]. The composed distribution thus captures the intersection of constraints, naturally framing action generation as constraint satisfaction while maintaining a probabilistic interpretation.

Denoising Diffusion Probabilistic Model (DDPM) framework [16] is adopted to model each component distribution $p_i(\mathbf{a}_{t,i}|\mathbf{o}_t)$. To sample from each component, we start from a noisy action sample $\mathbf{a}_{t,i}^K \sim \mathcal{N}(\mathbf{0}, \mathbf{I})$, and iteratively refine it using a noise prediction network $\varepsilon_{\theta_i}(\mathbf{a}_{t,i}^k, \mathbf{o}_t, k)$, progressively denoising over k steps:

$$\mathbf{a}_{t,i}^{k-1} = \alpha_k \left(\mathbf{a}_{t,i}^k - \gamma_k \, \boldsymbol{\varepsilon}_{\theta_i}(\mathbf{a}_{t,i}^k, \mathbf{o}_t, k) + \mathcal{N}(\mathbf{0}, \sigma_k^2 \mathbf{I}) \right), \quad (2)$$

where α_k , γ_k , and σ_k define the noise schedule. This process closely resembles Stochastic Langevin Dynamics [31], with ε_{θ_i} estimating the score function $\nabla \log p_i(\mathbf{a}_{t,i}|\mathbf{o}_t)$ [32].

Training of DDPM minimizes the mean squared error (MSE) between the true added noise ϵ^k and the network prediction:

$$\mathcal{L}_{\text{MSE}} = \|\boldsymbol{\epsilon}^k - \boldsymbol{\varepsilon}_{\theta}(\mathbf{a}_{t,i}^0 + \boldsymbol{\epsilon}^k, \mathbf{o}_t, k)\|_2^2, \quad (3)$$

where $\mathbf{a}_{t,i}^{0}$ is a clean trajectory sample valid under distribution $p_i(\mathbf{a}_{t,i}|\mathbf{o}_t)$. Minimizing this loss teaches the network

to progressively denoise noisy actions conditioned on observations.

B. Compositional Sampling and Routing

We next discuss how can we sample from the actual action distribution $p(\mathbf{a}_t | \mathbf{o}_t)$ given DDPM formulation of component distributions $\{p_i(\mathbf{a}_{t,i} | \mathbf{o}_t)\}$, as well as how to automatically discover each component distribution and optimize corresponding diffusion models jointly.

One way of viewing the composition of distributions is through the lens of energy-based models (EBM) [33]. Assume weights $\{w_{t,i}\}$ are given, and each weighted component distribution is parameterized as $p_i(\mathbf{a}_{t,i}|\mathbf{o}_t) \propto e^{-w_{t,i}E_i}$, then the actual action distribution can be expressed as $p(\mathbf{a}_t|\mathbf{o}_t) \propto e^{-\sum_i w_{t,i}E_i}$ [33]. Therefore, iterative sampling can be performed via Langevin dynamics:

$$\mathbf{a}_{t}^{k-1} = \mathbf{a}_{t}^{k} - \gamma_{k} \sum_{i} w_{t,i} \nabla_{\mathbf{a}_{t}^{k}} E_{i}(\mathbf{a}_{t}^{k}, \mathbf{o}_{t}) + \xi_{k}, \qquad (4)$$

where γ_k controls the step size and ξ_k introduces Gaussian noise. Note that we can bridge EBM with score-matching diffusion models [2, 11, 13, 34], which updates Equ. 4 as

$$\mathbf{a}_t^{k-1} = \mathbf{a}_t^k - \gamma_k \sum_i w_{t,i} \, \boldsymbol{\varepsilon}_{\theta_i}(\mathbf{a}_t^k, \mathbf{o}_t, k) + \xi_k.$$
 (5)

To optimize diffusion components jointly, we update MSE loss in Equ. 3 to

$$\mathcal{L}_{\text{MSE}} = \|\boldsymbol{\epsilon}^k - \sum_i w_{t,i} \,\boldsymbol{\varepsilon}_{\theta_i}(\mathbf{a}_t^0 + \boldsymbol{\epsilon}^k, \mathbf{o}_t, k)\|_2^2, \qquad (6)$$

where \mathbf{a}_t^0 is a demonstration trajectory sample. Then all diffusion components are optimized jointly end-to-end.

The weights $\{w_{t,i}\}\$ are predicted by a lightweight observation-conditioned neural network, referred to as *router*, which is optimized along with other diffusion components. This brings the last piece of FDP architecture. The pseudocode for training and inference are provided in Algo. 1 and Algo. 2.

Compared to discrete MoE routing, our compositional approach avoids routing instability and expert imbalance [6] by assigning continuous, observation-dependent weights to all components, rather than selecting a hard subset. In MoE, only a few experts are activated at each step, which can lead to underutilization of some experts and overfitting or saturation in others, especially when routing distributions are sharp or poorly calibrated. In contrast, our method aggregates contributions from all components via soft score-weighted composition, ensuring all modules remain active during optimization. Additionally, because all components participate in every training step, they receive gradient signals consistently, which encourages functional specialization.

C. Multitask Learning and Adaptation

Multitask Learning. This factorization is particularly wellsuited for multitask imitation learning, where action distributions are inherently multimodal due to diverse object properties, contact dynamics, and task goals. In contrast to monolithic policies that must capture all modes simultaneously, FDP distributes complexity evenly across diffusion components, each modeling a coherent subspace of behaviors. Unlike MoE policies, where skills may span combinations of experts across layers, our formulation yields interpretable and disentangled sub-skills.

Adapting to New Tasks. The modularity of FDP also enables efficient adaptation to unseen tasks. Instead of retraining the full model, we adapt by introducing a new diffusion component $\varepsilon_{\theta_{new}}$, initialized via *upcycling* [6] – copying weights from existing components. The updated score function becomes:

$$\varepsilon_{\text{adapt}}(\mathbf{a}_{t}^{k}, \mathbf{o}_{t}, k) = \sum_{i} w_{i} \,\varepsilon_{\theta_{i}}(\mathbf{a}_{t}^{k}, \mathbf{o}_{t}, k) + w_{\text{new}} \,\varepsilon_{\theta_{\text{new}}}(\mathbf{a}_{t}^{k}, \mathbf{o}_{t}, k),$$
(7)

where only $\varepsilon_{\theta_{new}}$ and the new router are updated during adaptation, using the training loss in Equ. 3. All previously trained components $\{\varepsilon_{\theta_i}\}$ are frozen. Freezing existing components ensures that the optimization focuses solely on capturing novel task dynamics without disrupting existing capabilities, thereby mitigating catastrophic forgetting. Such selective adaptation significantly reduces the number of trainable parameters and the amount of supervision required. In contrast, MoE models, where overlapping expert roles make modular reuse and analysis more difficult.

Finally, FDP supports heterogeneous architectures – diffusion models can vary in architecture and size, enabling scalable allocation of computation to match task complexity. This extensibility makes FDP broadly applicable in diverse and evolving robotic domains.

IV. EXPERIMENTS

In this section, we aim to empirically investigate several key questions regarding our proposed policy architecture: (1) Whether factorizing the complex action distribution into simpler distributions captured by smaller diffusion models can improve overall policy learning and performance. (2) Whether the modular structure of FDP, composed of multiple diffusionbased expert modules, facilitates more efficient and effective task transfer and adaptation. (3) How different adaptation strategies compare, highlighting trade-offs such as data efficiency, policy performance, and compute.

A. Experiments Setup

We evaluate policies on 16 tasks (Fig. 2) across Meta-World [14] and RLBench [15]. Demonstrations are generated by benchmark-provided scripted experts. Real-world experiments use a UR5e arm with a Robotiq gripper and a RealSense D415 camera (Fig. 3a). We evaluate policies on four distinct tasks: *cube red, cube blue, hang low,* and *hang high.* The tasks *cube-X* involve picking up a cube of color X from the tabletop and placing it into a designated bowl. The *hang-X* tasks require the robot to grasp a mug from the tabletop and precisely hang it on the X branch of a mug stand positioned on the table. Illustrations and setups of these real-world tasks are shown in Fig. 3. More details are provided in Appendix C.

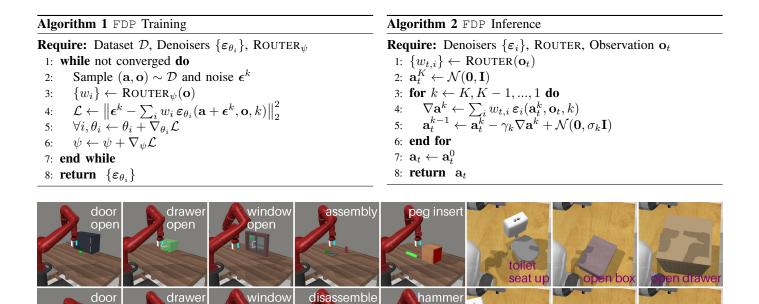


Fig. 2: Simulation environments. We evaluate FDP on 10 MetaWorld tasks and 6 RLBench tasks.

Fig. 3: Real-world setup and task illustrations. (a) Workspace setup with a UR5e arm, Robotiq gripper, and RealSense D415 camera. (b) High-level illustrations. Example rollouts can be found in Fig. 4.

(b) Illustration of hang-X

B. Implementations

close

RealSense

D415

close

UR5e

Robotiq

soft gripper

(a) Real-world workspace.

close

All policies take RGB images and joint angles as input and predict absolute joint angle trajectories. A history window of size 2 is used, with 16-step trajectories predicted and 8 steps executed. We use DDPM [16] with 100 diffusion steps during training and inference. We compare FDP against three baselines: DP [27], a monolithic diffusion policy; SDP [8], a MoE-based diffusion policy with observation-conditioned routing; and MoDE [9], a MoE variant with routing based on noise levels. Task-specific routing and goal conditioning are removed for fair comparison. We follow the original configurations used in each baselines, and proportionally reduce

the model size of MoDE to match others. We refer readers to the original papers for more details on architecture and training. In FDP, four U-Net diffusion modules are composed. For adaptation, we adopt the upcycling strategy [6] to initialize new MoE experts or diffusion components from existing ones. More details are available in Appendix D.

(c) Illustration of cube-X

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C. Multitask Learning

We first investigate whether decomposing complex motion distributions into simpler, behavior-specialized components can improve policy performance in multitask settings.

Simulation. We evaluate FDP on six MetaWorld tasks (25 demonstrations each) and four RLBench tasks (50 demonstra-

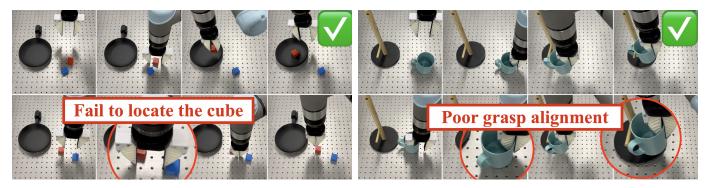


Fig. 4: Qualitative real-world rollouts. Each row shows execution for *cube-X* (left) and *hang-X* (right) tasks. Successes are shown in the top row; failure cases (bottom) illustrate challenges faced by baselines.

Policy	MetaWorld	RLBench
DP	0.725	0.569
SDP	0.717	0.319
MoDE	0.733	0.394
FDP	0.750	0.638

TABLE I: **Multitask learning in simulation.** Average success rate on MetaWorld (*door open, drawer open, assembly, window close, peg insert, hammer*) and RLBench (*toilet seat up, open box, open drawer, take umbrella out*) tasks. Evaluated over 40 episodes per task. See Table VI for full results.

tions each). All methods are evaluated over 40 rollouts per task, with results shown in Table I. The DP baseline performs surprisingly well, particularly on tasks like drawer open, assembly, and hammer, which primarily involve reaching and grasping and exhibit fewer multimodal behaviors - making them easier to solve with a single model. Among modular baselines, SDP underperforms due to instability common in training MoE architectures [6]: too few experts limit expressiveness, while too many can cause overfitting and noisy routing. MoDE performs reasonably by routing based on the noise level, but still inherits instability from MoE training [9]. In contrast, FDP's compositional structure avoids abrupt routing decisions by continuously composing diffusion component outputs via score-weighted aggregation, which enables stable training and more balanced component specialization of the multimodal action distributions.

Policy	Cube Red	Hang Low	Avg.
DP	0.700	0.800	0.750
SDP	0.750	0.650	0.700
MoDE	0.700	0.800	0.750
FDP	0.750	0.850	0.800

TABLE II: **Real-world multitask success rates.** Average over 20 trials. Tasks: *cube red* and *hang low*.

Real-world. We further evaluate our method in real-world settings on two tasks: *cube red* (300 demonstrations) and *hang low* (200 demonstrations). 20 samples are used for evaluation, and results are summarized in Table II. The DP baseline often overfits to specific joint trajectories, failing to attend to RGB inputs due to the multimodal and perceptually complex nature of the tasks. By contrast, FDP captures diverse behavior patterns more effectively by decomposing the action

distribution across interpretable sub-modules. This results in higher success rates. Fig. 4 shows qualitative failure cases from baseline methods, which struggle to capture the complex distribution, resulting in imprecise end-effector poses and frequent task failures.

D. Task Transfer and Adaptation

In this section, we evaluate the adaptability of FDP in adapting to novel tasks under limited data. We compare several adaptation strategies: full-parameter fine-tuning, partial finetuning of the router, observation encoder, and selective module expansion via new expert components.

Method	Policy	MetaWorld	RLBench
	DP	0.900	0.800
Full Param	SDP	0.892	0.763
Full Param.	MoDE	0.917	0.813
	FDP	0.917	0.825
	SDP	0.833	0.338
Router + Obs. Enc.	MoDE	0.833	0.438
	FDP	0.858	0.463
	SDP	0.900	0.450
+ New Module	MoDE	0.908	0.600
	FDP	0.925	0.850

TABLE III: Adaptation in MetaWorld (door open, drawer open, assembly, window close, peg insert, hammer) and RLBench (toilet seat up, open box, open drawer, take umbrella out). Pretrained on tasks in Table I. Full results in Table VII.

Simulation. We evaluate adaptation performance on four MetaWorld tasks and two RLBench tasks, using 10 and 25 demonstrations per task, respectively. We run 60 evaluations for MetaWorld and 40 evaluations for RLBench. As shown in Table III, full-parameter fine-tuning achieves strong performance but is computationally intensive. Partial fine-tuning – modifying only the router or including the observation encoder – offers limited gains. In contrast, adding new modules (two expert blocks per layer for MoE-based methods and a new diffusion component for FDP) consistently improves performance. FDP benefits most from this strategy, leveraging its compositional structure to reuse prior knowledge while efficiently learning new behaviors.

Real-world. We further evaluate adaptation on two realworld tasks, each with 100 demonstrations. 20 samples are

Method	Policy	Cube Blue	Hang High	Avg.
Full Param.	DP	0.750	0.850	0.800
	SDP	0.700	0.800	0.750
	MoDE	0.750	0.800	0.775
	FDP	0.850	0.750	0.800
Router + Obs. Enc.	SDP	0.500	0.450	0.475
	MoDE	0.500	0.550	0.525
	FDP	0.550	0.550	0.550
+ New Module	SDP	0.650	0.550	0.600
	MoDE	0.700	0.650	0.675
	FDP	0.850	0.850	0.850

TABLE IV: Adaptation in real-world. Evaluated on *cube blue* and *hang high*. Pretrained on *cube red* and *hang low*. See Table VIII for full results.

used for evaluation. Results in Table IV echo the simulation trends. While full-parameter fine-tuning performs reasonably well, it is resource-intensive. Partial fine-tuning yields modest improvements. The most effective strategy across all methods involves introducing new modules. Under this setting, FDP achieves the best performance, highlighting the advantage of its modular design for rapid and robust adaptation even in complex, real-world scenarios.

V. ANALYSIS

A. Scaling of Number of Diffusion Components

We study how the number of diffusion components in FDP affects multitask performance. Experiments are conducted on selected tasks from MetaWorld (*door close, drawer close, disassemble, window open*) and RLBench (*toilet seat up, open box, open drawer, take umbrella out*). As shown in Table V, increasing the number of components from 2 to 4 consistently improves performance, indicating greater expressiveness and better sub-skill specialization. Beyond 4 components, performance plateaus, suggesting diminishing returns. Overall, 4 components provide a good trade-off between model complexity and performance for the tasks considered. We recommend using 4 components as a reasonable starting point, though some hyperparameter tuning may improve performance.

# Comp	MetaWorld	RLBench
2	0.867	0.544
3	0.900	0.588
4	0.913	0.638
5	0.913	0.644
6	0.917	0.650
7	0.919	0.656

TABLE V: Multitask performance of FDP with different numbers of components on MetaWorld and RLBench. Performance improves up to 4 components and plateaus thereafter.

B. Scaling of Number of Demonstrations

Multitask Learning. We evaluate how FDP benefits from increasing amounts of demonstration data. As shown in Fig. 5a, performance improves steadily with more demonstrations. FDP consistently outperforms baselines, with particularly large gains on RLBench where complex, contact-rich interactions make effective decomposition especially valuable.

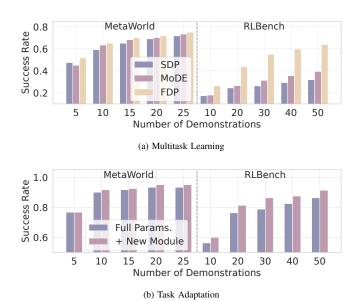


Fig. 5: **Performance scaling with number of demonstrations. (a)** Multitask learning success rate of FDP across tasks listed in Table I. **(b)** Task adaptation performance on tasks from Table III.

Task Adaptation. We analyze how adaptation performance scales with the number of demonstrations, and compare the proposed + *New Module* strategy with full-parameter fine-tuning. As shown in Fig. 5b, both strategies benefit from more data, but + *New Module* achieves comparable or better performance with even fewer demonstrations (on RLBench). This highlights the strength of our modular design in enabling data-efficient adaptation while avoiding the cost and potential catastrophic forgetting associated with updating all model parameters.

C. Diffusion Components Analysis

To better understand how modularity manifests in FDP, we analyze the behavior and specialization of individual diffusion components. Fig. 7 shows rollout trajectories produced by each component in two representative MetaWorld tasks: *assembly* and *hammer*. Across both tasks, we observe that different components specialize in distinct functional stages, such as alignment, approach, and grasp execution. This consistent division of responsibility indicates that FDP naturally decomposes complex behaviors into distinct, interpretable sub-skills across its components.

To complement the qualitative analysis, we compute the pairwise cosine similarity between the score outputs, shown in Fig. 8, visualize how the learned components relate to each other during inference. While the components are not completely orthogonal, we observe noticeable variation between different pairs, indicating that diffusion components capture distinct, though partially overlapping, aspects of the behavior distribution.

FDP's structure contrasts with baseline MoE-based policies. In MoDE, experts specialize according to diffusion noise levels rather than task semantics, leading to noise-level specialization that lacks behavioral interpretability. In SDP, sub-skills emerge

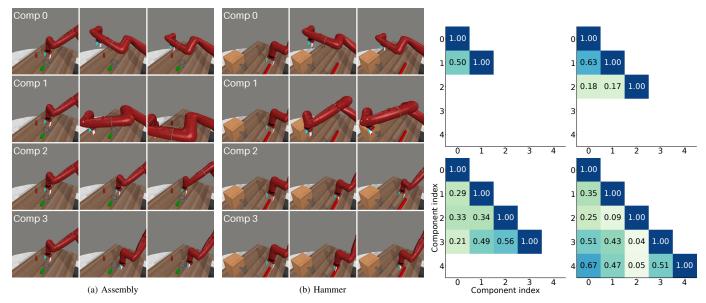


Fig. 7: Rollout trajectories of individual diffusion components in FDP. (a) In assembly, Fig. 8: Cosine similarity between diffusion component components 0 and 1 align the robot with the stand, component 2 aligns with the ring, and scores. Each heatmap shows average pairwise similarity for component 3 executes the grasp. (b) In hammer, components 0 and 1 align and approach models with 2-5 components, computed over four RLBench the pin, component 2 approaches the hammer, and component 3 performs the grasp. Enlarged version in Fig. 9.

tasks. Lower similarity indicates more distinct component behaviors.

from sets of experts selected across layers, making it difficult to assign functionality to any single expert. Experts can be reused across different combinations or ignored altogether. Furthermore, SDP routers tend to favor a small subset of experts, leading to poor load balancing and limited diversity [8]. FDP assigns each behavioral mode to a distinct, standalone diffusion component. This enables clean semantic separation between modules, avoiding routing instability or expert redundancy commonly seen in MoE. This modular design facilitates straightforward analysis, interpretability, and reuse, contributing to better training stability and more coherent specialization.

VI. CONCLUSION

We present FDP, a modular policy architecture that leverages factorized diffusion models for multitask imitation learning and efficient task adaptation. By composing behaviorspecialized diffusion components, our method improves generalization, interpretability, and modularity over prior approaches. Extensive experiments on both simulated and realworld tasks demonstrate that FDP outperforms strong baselines in multitask performance and adapts effectively to new tasks. We believe our work highlights the value of compositional structure and offers a scalable framework for building generalpurpose robotic agents.

VII. LIMITATIONS

While our work demonstrates clear modular specialization, there remain interesting directions for further analysis. First, we currently use homogeneous diffusion components of similar architecture and size. Future work could explore heterogeneous module designs, such as mixing U-Net and Transformerbased diffusion models, or using modules of varying sizes, to enhance flexibility and expressiveness. Second, we primarily study specialization through rollout visualization; an alternative approach is to systematically remove individual diffusion components and observe the resulting policy behaviors and failure modes. This could provide deeper insights into the roles and dependencies of different sub-skills captured by the factorized policy.

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APPENDIX

A. Background on Diffusion Policy

Our method, FDP, builds upon the diffusion policy framework [35], leveraging U-Net-based denoising models to represent the conditional action distribution. Diffusion models are a class of generative models that synthesize samples by reversing a predefined noise process. Specifically, we adopt the Denoising Diffusion Probabilistic Model (DDPM) [16] to model the policy $\pi_{\theta}(\mathbf{a}_t | \mathbf{o}_t)$, where \mathbf{o}_t denotes the observation and \mathbf{a}_t the action.

Sampling begins with a Gaussian noise $\mathbf{a}^K \sim \mathcal{N}(\mathbf{0}, \mathbf{I})$ and proceeds through a sequence of denoising steps using a noise prediction network ε_{θ} :

$$\mathbf{a}^{k-1} = \alpha_k \left(\mathbf{a}^k - \gamma_k \,\boldsymbol{\varepsilon}_{\theta}(\mathbf{a}^k, \mathbf{o}, k) + \mathcal{N}(\mathbf{0}, \sigma_k^2 \mathbf{I}) \right), \quad (8)$$

where α_k , γ_k , and σ_k define the noise schedule at timestep k. This denoising process is akin to Stochastic Langevin Dynamics [31], where ε_{θ} approximates the score function $\nabla \log p(\mathbf{a}|\mathbf{o})$ of an implicit energy-based model [32].

During training, the model learns to predict the added noise. A clean action trajectory \mathbf{a}^0 is perturbed by Gaussian noise $\boldsymbol{\epsilon}^k$ to form a noisy sample $\mathbf{a}^k = \mathbf{a}^0 + \boldsymbol{\epsilon}^k$. The network is then supervised to reconstruct the noise via a mean squared error objective:

$$\mathcal{L}_{\text{MSE}} = \left\| \boldsymbol{\epsilon}^k - \boldsymbol{\varepsilon}_{\theta}(\mathbf{a}^k, \mathbf{o}, k) \right\|_2^2.$$
(9)

Minimizing this loss teaches the network to recover the denoising direction, enabling generation of coherent, observation-conditioned action sequences through iterative refinement.

B. Background on Compositional Sampling

Compositional generation with diffusion models has gained increasing attention in robotics and generative modeling due to its ability to produce structured, interpretable outputs. By combining modular distributions, this approach offers enhanced flexibility and expressiveness for tasks such as robot trajectory generation and image synthesis [2, 11, 34, 13].

A core theoretical insight is that aggregating diffusion scores is equivalent to sampling from the product of the underlying probability distributions. Let p_1, p_2, \ldots, p_n be a set of component distributions. Their product distribution is given by:

$$p_{\text{product}}(\mathbf{x}) \propto \prod_{i=1}^{n} p_i(\mathbf{x}),$$
 (10)

which assigns high probability to samples that are simultaneously likely under all component distributions - i.e., it captures their intersection.

In the energy-based formulation, each $p_i(\mathbf{x}) \propto \exp(-E_i(\mathbf{x}))$, and their product yields a new energy-based model:

$$p_{\text{product}}(\mathbf{x}) \propto \exp\left(-\sum_{i=1}^{n} E_i(\mathbf{x})\right)$$
 [33]. (11)

Sampling from p_{product} can be performed using Langevin dynamics. Starting from an initial noisy sample $\mathbf{x}^K \sim \mathcal{N}(\mathbf{0}, \mathbf{I})$, the iterative update is:

$$\mathbf{x}^{k-1} = \mathbf{x}^k - \gamma_k \nabla_{\mathbf{x}} E_{\text{product}}(\mathbf{x}^k) + \xi_k \tag{12}$$

$$=\mathbf{x}^{k}-\gamma_{k}\sum_{i}\nabla_{\mathbf{x}}E_{i}(\mathbf{x}^{k})+\xi_{k},$$
(13)

where γ_k is the step size and $\xi_k \sim \mathcal{N}(\mathbf{0}, \sigma_k^2 \mathbf{I})$ adds stochasticity to improve exploration. One can bridge EBM and score-matching diffusion [11].

Compositional sampling enables several practical benefits. It enhances robustness by enforcing agreement across component models, which helps reduce uncertainty and improves sample fidelity. Moreover, it facilitates modular design – independently trained components can be integrated at inference time, promoting scalability across diverse tasks and data domains [2, 11].

C. Experiment Setup

Simulation. We evaluate FDP on two widely used robotic manipulation benchmarks: MetaWorld [14] and RLBench [15], each based on a distinct physics engine. MetaWorld, built on MuJoCo [36], offers 50 diverse tasks; we select 10 representative ones focused on object reconfiguration and tool use. RLBench, running on CoppeliaSim [37], includes over 100 tasks; we select 6 involving contact-rich and articulated-object interactions. In total, we evaluate across 16 tasks (see Fig. 2). Expert demonstrations are generated using the scripted policies provided by each benchmark.

Real-world. Real-world experiments are conducted using a UR5e robotic arm equipped with a Robotiq soft gripper and a front-facing RealSense D415 camera (Fig. 3a). All objects are custom-designed and 3D printed to ensure controlled and reproducible conditions. We consider four real-world tasks: *cube red, cube blue, hang low,* and *hang high*. The *cube-X* tasks require picking up a colored cube from the table and placing it in a target bowl. The *hang-X* tasks involve grasping a mug and precisely hanging it on the corresponding branch of a mug stand. Task setups and illustrations are shown in Fig. 3.

D. Implementation Details

Overview. All policies take RGB images and joint angles as input and predict trajectories of absolute joint angles. A history window of size 2 is used, and each model predicts a 16-step trajectory, from which the first 8 actions are executed. We adopt the DDPM framework [16] with 100 diffusion steps during both training and inference. All models are trained for the same number of gradient steps. No task identity is provided—there is no task-conditioning or task-specific routing in any policy.

Baselines. We compare against three existing approaches. DP [27] is a monolithic U-Net-based policy without modular structure. SDP [8] introduces a Mixture-of-Experts (MoE) architecture with expert selection based on observations. MoDE [9] also uses an MoE design but routes experts based on the diffusion noise level. For fair comparison, we remove taskspecific routers from SDP and task-goal conditioning from MoDE, ensuring that all baselines rely solely on observations. We follow original architecture configurations: four experts per layer with two selected per forward pass, and proportionally reduce MoDE model size to match the others. For additional architectural and training details, we refer readers to the respective papers.

FDP. Our method, FDP, explicitly factorizes the policy into four U-Net-based diffusion components. These modules are trained jointly and composed through score aggregation using mixture weights generated by a two-layer MLP router conditioned on observations.

Adaptation. For the + *New Module* strategy, we adopt the upcycling approach [6], where new components are initialized by copying weights from randomly selected existing modules. In SDP and MoDE, adaptation involves adding two new upcycled expert blocks per MoE layer, FDP adds one new U-Net diffusion component.

E. Additional Results on Multitask Learning

We provide detailed results for multitask learning across all MetaWorld and RLBench tasks evaluated in our experiments. Table VI shows per-task success rates and overall averages over 40 evaluation rollouts per task. While most baselines perform reasonably well on simpler tasks such as *door open* and *drawer open*, they tend to underperform on tasks that require more precise coordination or complex spatial reasoning (e.g., *peg insert, take umbrella out*). Our method, FDP, consistently achieves strong performance across all tasks, benefiting from its modular structure and better sub-skill decomposition.

In particular, on RLBench tasks, where action distributions are more multimodal and contact-rich, FDP outperforms others by a significant margin. This suggests improved capacity for modeling diverse behaviors and generalizing across complex task structures.

To further illustrate the advantages of our approach, Fig. 4 presents qualitative comparisons of real-world rollouts. Successful trials are shown in the top rows, while failure cases (bottom rows) highlight common errors made by baseline methods, such as imprecise end-effector poses and grasp failures. FDP consistently produces robust and accurate execution across task variants.

F. Additional Results on Task Adaptation

We report detailed task-wise results for adaptation experiments in both simulation and real-world settings.

Tables VII and VIII present full adaptation results for both simulation and real-world settings. In simulation, FDP achieves the highest average success rate across both Meta-World and RLBench when using the + *New Module* adaptation strategy, indicating its superior ability to incorporate new task knowledge without disrupting prior components.

Notably, FDP achieves strong performance even when only the router and observation encoder are updated, outperforming SDP and MoDE by a significant margin. This implies that

MetaWorld							
Policy	Door Open	Drawer Open	Assembly	Window Close	Peg Insert	Hammer	Avg.
DP	0.900	1.000	1.000	0.950	0.250	0.250	0.725
SDP	0.900	1.000	1.000	1.000	0.200	0.200	0.717
MoDE	1.000	1.000	0.950	1.000	0.200	0.250	0.733
FDP	1.000	1.000	1.000	1.000	0.250	0.250	0.750
Policy	RLBench Policy Toilet Seat Up Open Box Open Drawer Take Umbrella Out Avg.						
	0.500	0.925	0.800	0.100			-
DP	0.500	0.825	0.800	0.100			0.569
SDP	0.425	0.775	0.025	0.050			0.319
MoDE	0.450	0.500	0.475	0.150			0.394
FDP	0.500	0.900	0.800	0.350			0.638

TABLE VI: Multitask learning evaluation on MetaWorld and RLBench. We report average success rate over 40 samples.

	MetaWorld				RLB	lench			
Method	Policy	Door Close	Drawer Close	Disassemble	Window Open	Avg.	Toilet Seat Down	Close Box	Avg.
	DP	1.000	1.000	0.600	1.000	0.900	0.900	0.700	0.800
Full	SDP	0.933	1.000	0.633	1.000	0.892	0.950	0.575	0.763
Parameter	MoDE	1.000	1.000	0.667	1.000	0.917	0.925	0.700	0.813
	FDP	1.000	1.000	0.667	1.000	0.917	0.800	0.850	0.825
	SDP	0.733	0.000	0.000	0.067	0.200	0.200	0.025	0.113
Router	MoDE	0.000	0.000	0.000	0.267	0.067	0.100	0.000	0.050
	FDP	0.867	0.667	0.000	0.067	0.400	0.150	0.000	0.075
+ Observation	SDP	1.000	1.000	0.333	1.000	0.833	0.525	0.150	0.338
+ Observation Encoder	MoDE	0.933	1.000	0.400	1.000	0.833	0.675	0.200	0.438
Elicodei	FDP	1.000	0.933	0.500	1.000	0.858	0.650	0.275	0.463
+ New	SDP	1.000	1.000	0.600	1.000	0.900	0.675	0.225	0.450
Module	MoDE	1.000	1.000	0.633	1.000	0.908	0.825	0.375	0.600
wiodule	FDP	1.000	1.000	0.700	1.000	0.925	0.925	0.775	0.850

TABLE VII: Adaptation evaluation on MetaWorld and RLBench. Pretrained on tasks shown in Table VI. We report average success rate on 60 MetaWorld samples and 40 RLBench samples.

Method	Policy	Cube Blue	Hang High	Avg.
Full Parameter	DP SDP MoDE FDP	0.750 0.700 0.750 0.850	0.850 0.800 0.800 0.750	0.800 0.750 0.775 0.800
Router	SDP MoDE FDP	0.000 0.100 0.050	0.100 0.050 0.100	0.050 0.075 0.075
+ Observation Encoder	SDP MoDE FDP	0.500 0.500 0.550	0.450 0.550 0.550	0.475 0.525 0.550
+ New Module	SDP MoDE FDP	0.650 0.700 0.850	0.550 0.650 0.850	0.600 0.675 0.850

TABLE VIII: Adaptation evaluation in real-world. Pretrained on tasks shown in Table II. We report average success rate on 20 samples.

the component distributions in FDP are more reusable and interpretable than those in other modular methods, which often rely on entangled expert combinations.

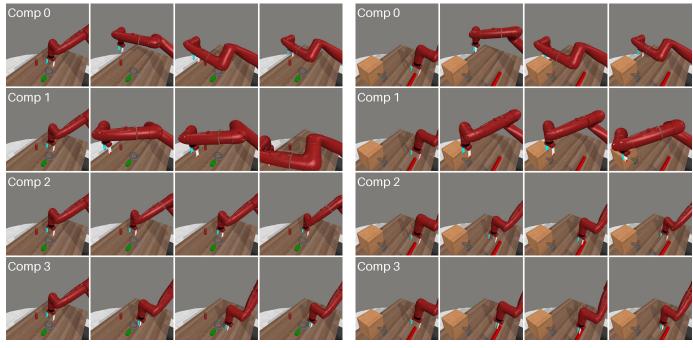
In real-world experiments, we observe similar trends: FDP consistently performs better or matches the best baseline across various adaptation settings. These results highlight FDP 's practical advantages for continual learning and real-world deployment, where quick adaptation to novel tasks with limited supervision is critical.

G. Diffusion Components Analysis

We provide enlarged visualizations of rollout trajectories for each diffusion component in FDP to complement the compressed figure shown in the main paper (Fig. 7). As depicted in Fig. 9, each component learns to specialize in a distinct sub-skill, validating the modular structure of our approach.

In the *assembly* task, components 0 and 1 guide the robot to align with the assembly stand, component 2 adjusts the end-effector position to align with the ring, and component 3 performs the grasping motion. In the *hammer* task, components 0 and 1 coordinate to align and approach the pin, component 2 transitions the arm toward the hammer, and component 3 executes the grasp. Notably, each component displays temporally consistent behavior, and their combined outputs lead to successful task execution. This clear division of responsibility reflects meaningful behavioral decomposition, with each component contributing a targeted motion primitive.

This visualization confirms that the learned components are functionally interpretable and behaviorally distinct. Unlike MoE-based baselines, where experts are reused across skills in entangled ways, our method enables disentangled, reusable skill modules.



(a) Assembly

(b) Hammer

Fig. 9: Rollout trajectories of individual diffusion components in FDP. (a) In *assembly*, components 0 and 1 align the robot with the stand, component 2 aligns with the ring, and component 3 executes the grasp. (b) In *hammer*, components 0 and 1 align and approach the pin, component 2 approaches the hammer, and component 3 performs the grasp. Checkout videos on factorized-diffusion-policy.github.io.

H. Training Convergence

We compare the training efficiency of FDP against MoDE and SDP by analyzing convergence curves on validation trajectories. Specifically, we track the mean squared error (MSE) loss used during diffusion training, measured over validation episodes across training epochs. Results are shown in Fig. 10 for both MetaWorld and RLBench tasks.

FDP consistently achieves lower validation MSE in fewer epochs, indicating faster convergence. MoDE converges more slowly, while SDP shows higher variance and slower reduction in loss, likely due to instability in expert selection and poor load balancing during training. These results support our claim that continuous score composition in FDP improves optimization stability compared to discrete Mixture-of-Expert (MoE) methods.

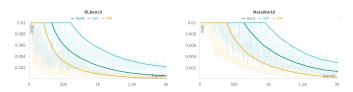


Fig. 10: **Training convergence curves**. Mean squared error (MSE) loss over training epochs for RLBench and MetaWorld tasks. FDP consistently converges faster and more stably than MoDE and SDP, indicating improved training efficiency and optimization stability.

I. Rollout Visualizations

We present additional qualitative results to illustrate the behavior of our policy FDP across diverse manipulation tasks

in both simulation and real-world. Fig. 11 shows rollout sequences captured from different stages of task execution. These filmstrips visualize the robot's actions from the initial observation to successful task completion. Tasks involve reaching, aligning, grasping, and manipulating articulated or occluded objects. The qualitative rollouts reinforce the quantitative findings and further validate that compositional policy factorization leads to coherent, interpretable, and reusable behavior modules.

door open	door close
drawer open	drawer close
window open	window close
assembly	disassemble
K K K	
toilet seat up oppon box	toilet seat down close box
open bex open drawer open drawer	
cube red	take umbr- ella out
hang low	hang high

Fig. 11: Example rollout sequences for various tasks. Each filmstrip visualizes the trajectory execution of a policy on a specific manipulation task, highlighting the key interaction stages from initial observation to task completion. Checkout videos on factorized-diffusion-policy.github.io.